



# AIMS

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## MISG 2019: ONLINE AUCTION DESIGN

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# Aim

## Primary

Can we design an **on-line** auction to incorporate **interesting features** whilst maintaining **required behaviour**?

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## Primary

Can we design an **on-line** auction to incorporate **interesting features** whilst maintaining **required behaviour**?

## Secondary

What new possibilities does on-line offer?

## Recap: Auction Formalisation in Z

- Formal specification of a **A**bstract **D**ata **T**ype (ADT)
- ADT consists of a set and operations on set
- Used to specify state, and how state updates
- Discrete analog to a continuous dynamical system

*See appendix for the Z specification of an English auction*

# Online Auction Characteristics

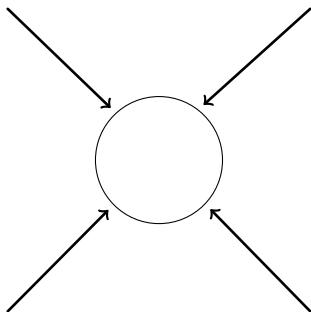
## Unique Aspects of an Online Auction:

- increased number of players
- multiple simultaneous auctions (decentralisation)
- reduced costs increase payoffs
- information availability
- security requirements

# Centralized System

What is a centralized system?

- A client/server architecture
- All communication goes through a single node
- All computation is done on a single server



# Centralized System

Advantages of centralized system:

- Simple implementation
- Maximize data integrity and reduce data redundancy
- Subject to location
- Updates to any given set of data are immediately received by every end-user

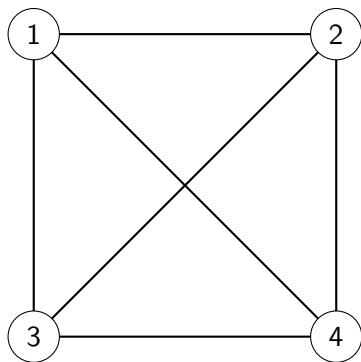


# Centralized System

Disadvantages of centralized system:

- Server bottleneck
- If the server goes down, the platform goes down
- Single source of failure and attack.

# Decentralized System



- System whose components are located on different computers
- Communication is done by passing messages

# Decentralized System

Advantages of Decentralized system:

- Eliminating single source
- Distribute the load between the nodes
- If a node goes down, the platform still works
- Every node has all the information

# Decentralized System

## Challenges of Decentralized System:

- Lack of global clock
- Maintaining consistency
- Network communication
- Complicated

# How does it work?

Maintaining time:

# How does it work?

Maintaining time:

- Universal time, e.g. GMT
- Nodes have regional time zone and system converts it to GMT
- Bidding happens on the same instance universally
- Deadline is then universal

# Communication example

How does one guarantee consistency between nodes?

# Communication example

How does one guarantee consistency between nodes?

- All the nodes need the same information
- But there is no central node to orchestrate this
- Solution: Communication!



# Communication example

## Checkpoint 1

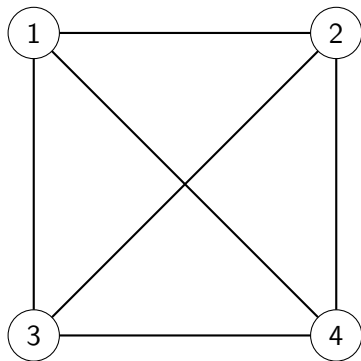


Figure: *Time: 10 : 00, Price: R100*

# Communication example

**Bid at node 1:** *Time:* 10 : 10, *Price:* R150

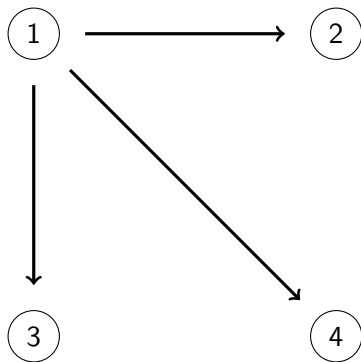


Figure: Broadcasting information from node 1

# Communication example

**Bid at node 1:** *Time:* 10 : 10, *Price:* R150

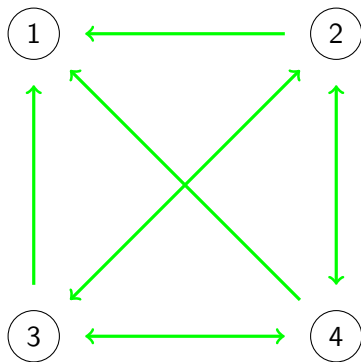


Figure: Broadcasting replies from other nodes

## Communication example

As soon as a node receives 3 acceptance broadcasts (including its own), the node updates the new checkpoint:

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### Checkpoint 2

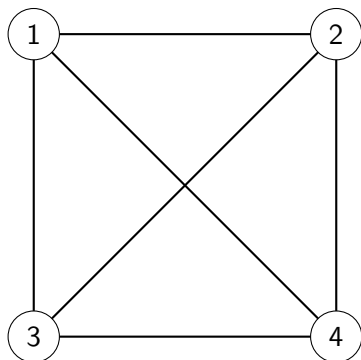


Figure: *Time: 10 : 10, Price: R150*

# Communication example

What can go wrong?

## Communication example

What can go wrong?

**Bid at node 2:** *Time:* 10 : 20, *Price:* R200

**Bid at node 3:** *Time:* 10 : 21, *Price:* R220

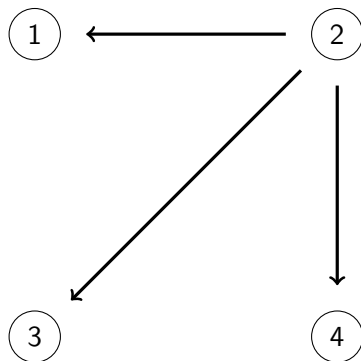


Figure: Broadcasting information from node 2

## Communication example

**Bid at node 2:** *Time:* 10 : 20, *Price:* R200 (Rejected)

**Bid at node 3:** *Time:* 10 : 21, *Price:* R220

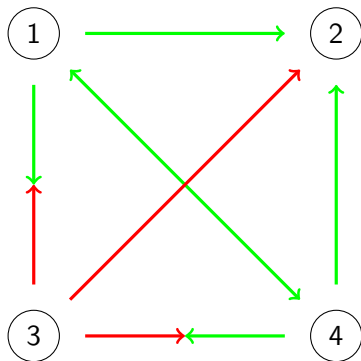


Figure: Broadcasting replies from other nodes



## Communication example

**Bid at node 2:** *Time:* 10 : 20, *Price:* R200

**Bid at node 3:** *Time:* 10 : 21, *Price:* R220 (Accepted)

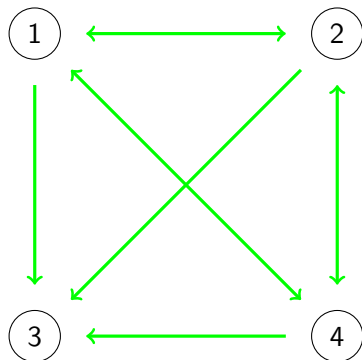


Figure: Broadcasting replies from other nodes

# Communication example

## Checkpoint 3

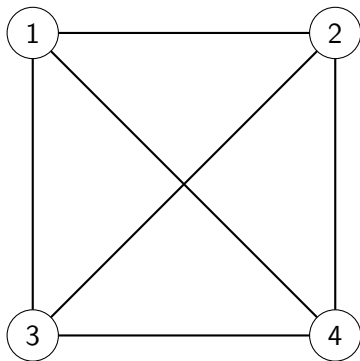


Figure: *Time: 10 : 20, Price: R220*

# Node buffering

What if a new bid comes in while the previous bid is still being processed?

## Node buffering

What if a new bid comes in while the previous bid is still being processed?

- **Processing bid at node 3:** *Time: 10 : 21, Price: R220*
- **New bid at node 3:** *Time: 10 : 22, Price: R250*

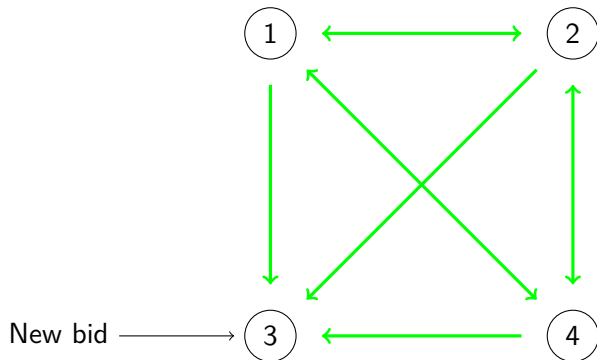


Figure: Broadcasting replies from other nodes

# Node buffering

What if a new bid comes in while the previous bid is still being processed?

- **Processing bid at node 3:** *Time: 10 : 21, Price: R220*
- **New bid at node 3:** *Time: 10 : 22, Price: R250*

# Node buffering

What if a new bid comes in while the previous bid is still being processed?

- **Processing bid at node 3:** *Time: 10 : 21, Price: R220*
- **New bid at node 3:** *Time: 10 : 22, Price: R250*

The new bid is buffered. This means the system first finishes its current process, before node 3 again sends the information on the new bid to the other nodes

# Node delay

- What if a node goes down and does not reply?

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# Node delay

- What if a node goes down and does not reply?
- The system will have a preset time in which each node has to reply
- If the node does not reply in time, the system will continue without it
- If the node comes back online, then it simply gets updated with the current checkpoint

# The deadline

How does the system handle the deadline with communication delays?

# The deadline

How does the system handle the deadline with communication delays?

- There is a soft deadline and a hard deadline
- The soft deadline occurs when the GMT deadline is reached at each node
- No bids can be played after this at any node

# The deadline

- There is also a hard deadline

# The deadline

- There is also a hard deadline
- After the hard deadline, a final checkpoint is reached
- This deadline is used by the system to sort out the last unsaved bids
- It gives time for delayed last bids to come through
- After the hard deadline is reached, a winner is announced

# Exploiting Information

The **online** aspect allows for data to be captured. Data includes historical auction data and meta-data.

Information is communal in a decentralised system and can be used to improve functioning of the network.

Information can be used to:

- inform and improve additional features: security, system integrity
- (network-level) Improve matching of buyers and sellers
- (auction-level) Inform decisions for buyers and sellers

## Network-level Information

- “Success” of the network system can be measured by the number of auctions
- Each auction implies a positive (possibly asymmetric) payoff for both the winning bidder and seller
- Auction parameters and controls can be learned to maximize the number of auctions.
- The result is improved (decentralized) matching of buyers and sellers

## Auction-level Information

Suggestions to 3 stakeholder types - Buyers , Sellers, Manufacturers  
Retailers




- Information for prospective retailers: show items that are selling
- Assumption of an auction: sellers sell high and buyers buy low.  
Information for seller: probability of making a sale based on empirical evidence (how well product is doing)
- Can use regression analysis to plot price of goods vs probability of it being sold and provide that information to prospective sellers
- Informs a plot: `rest_series.html`



# Conclusion

- Auction fundamentals and formalisation of the information system - Z Notation
- Online allows for Decentralisation
- Data can be used to improve network functioning and bidder strategies
- Prove the chosen auction design behaves as desired

# References

-  Chapter 9, Auctions, in *Networks, Crowds and Markets: Reasoning about a Highly Connected World*. D. Easley and J. Kleinberg. CUP, 2010. [www.cs.cornell.edu/home/kleinber/networks-book/](http://www.cs.cornell.edu/home/kleinber/networks-book/)
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# Z Notation

- Formal Specification
- Reference of point for: Analyzer, Programmer, Tester and Documentary
- Decomposing the specification into schemes
- Describing the static and dynamic aspect of the system.

# Auctions Framework By Example

*Auction*

Condition regarding stored inputs  
*seller, cbuyer* :  $\mathbb{U}$

*INIT*

*State*

Interaction between the variables

## Feature Example: State

### State

$\Delta seller, cbuyer : \mathbb{U}$

$item : \mathbb{I}$

$history : seq\ BIDS$

$cbid : \mathbb{R}^+$

$scost : \mathbb{B}$

$dline : \mathbb{T}$

$sp : \mathbb{R}^+$

$inc : \mathbb{R}^+$

$systime : \mathbb{T}$

$cbuyer = history[-1] \cdot u?$

$cbid = history[-1] \cdot price?$

## Feature Example: Bids

*Bids*

$\Delta State$

$cbuyer? : \mathbb{U}$

$cprice? : \mathbb{R}^+$

$btime? : \mathbb{T}$

$price? \geq cbid + inc$

$sytime \leq btime < dline$

$history' = history + [cbuyer?, price?, btime?]$

## Feature Example: Init

*INIT*

*State'*

*seller?* :  $\mathbb{U}$

*sp?* :  $\mathbb{R}^+$

*inc?* :  $\mathbb{R}^+$

*item?* :  $\mathbb{I}$

*dline?* :  $\mathbb{T}$

*cbid?* :  $\mathbb{R}^+$

*ctime!* :  $\mathbb{T}$

*scost?* :  $\mathbb{B}$

*cbuyer'* = []

*history'* = []

*cbid!* = *cbid'* = *sp?*

*ctime!* = *systemtime*

## Feature Example: Init (Continued)

$inc > 0$

$scost' = scost?$



# Feature Example: USERINFO

U

*username*

*uid*

*bankdetails*

*contactdetails*

\* \* \*

# Feature Example: ITEM

II

*picture*  
*description*  
*location*

\* \* \*

## Feature Example: END

*END*

$\exists$ State

*cbuyer!*

*price!*

*btime!*

*sysTime = dline*  $\Rightarrow$

*cbuyer!* = *history*[-1] · *cbuyer*

*price!* = *history*[-1] · *price*

*btime!* = *history*[-1] · *btime*